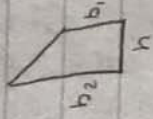


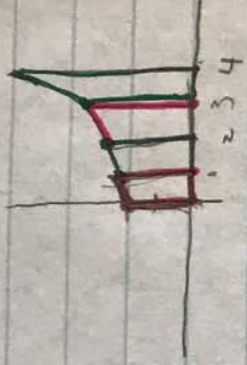
5.9 Approx. integration

$$A_{\text{trap}} = \frac{1}{2} \cdot h \cdot (b_1 + b_2)$$



ex: find the area under the curve of the function
 $y = \frac{1}{4}x^2 + 2$ $[0, 4]$

$$\int_0^4 \left(\frac{1}{4}x^2 + 2 \right) dx$$



for evenly spaced intervals

$$h = \Delta x = \frac{b-a}{n}$$

Trapezoidal Rule

$$\int_a^b f(x) dx \approx T_n = \frac{\Delta x}{2} [f(x_0) + 2f(x_1) + 2f(x_2) + \dots + 2f(x_{n-1}) + f(x_n)]$$

$$\Delta x = \frac{4-0}{4} = 1$$

$$\begin{aligned} T_4 &= \frac{1}{2}(1) [f(0) + 2f(1) + 2f(2) + 2f(3) + f(4)] \\ &\approx \frac{1}{2} [2 + 2(2.25) + 2(3) + 2(4.25) + 6] \\ &\approx 13.5 \end{aligned}$$

Midpoint Rule

$$\int_a^b f(x) dx \approx M_n = \Delta x [f(\bar{x}_1) + f(\bar{x}_2) + \dots + f(\bar{x}_n)]$$

where $\Delta x = \frac{b-a}{n}$